P.O.C.A. WONG SIU CHING SECONDARY SCHOOL

## PURE MATHEMATICS

ALGEBRA I: POLYNOMIALS
ASSIGNMENT 6

| Date | Name | Grade / Score |
| :---: | :---: | :---: |
|  |  | $/ \mathbf{1 5}$ |

1. Let $P_{n}(x)=\cos \left(n \cos ^{-1} x\right)$, where $-1 \leq x \leq 1$ and $n$ is a non-negative integer.
(8 marks)
(a) Prove that $P_{n+1}(x)=2 x P_{n}(x)-P_{n-1}(x)$.
(b) Using induction to show that $P_{n}(x)$ is polynomial in $x$ of degree $n$ with leading coefficient $2^{n-1}$, for $n \geq 1$.
2. Given that $f(x)=4 x^{4}-2 x^{3}-16 x^{2}+5 x+9$ and $g(x)=2 x^{3}-x^{2}-5 x+4$. Find the G.C.D. $d(x)$ of $f(x)$ and $g(x)$ and find polynomials $u(x)$ and $v(x)$ such that $d(x)=u(x) f(x)+v(x) g(x)$.
(8 marks)
